

## ***A Theoretical Method for Calculating the Required Force in Front of a Bulldozer- Blade***

*Asst. Prof. Dr .Fahim Alhimdani,  
Mech. Eng. Dep.  
College of Engineering  
Al-Mustansiriya Univ.*

*Asst. Lec. Munaf Fathi Badr  
Mech. Eng. Dep.  
College of Engineering  
Al-Mustansiriya Univ.*

*Eng. Abeer Hashim,  
Mech. Eng. Dep.  
College of Engineering  
Al-Mustansiriya Univ.*

### **Abstract**

*This paper presents a theoretical approach for estimating the draught force in front of a bulldozer blade. Forces required to produce any kind of soil failure can be described by an additive equation. Advantage was taken by Reece's family of curves from which will be possible to obtain a ready solution to most two – dimensional passive pressure problems. An equation has been simplified making certain assumptions. Then an example for application was solved obtaining the required power for bulldozer to do a certain job. It is hoped that this paper will be useful, especially when choosing the right design of a bulldozer blade for a required purpose*

### **الخلاصة**

*أن هذا البحث يتعلق بكيفية حساب القوة اللازمة للدفع أمام السكينة في البلدوزر نظريا ولقد استخدمت منحنيات "ريز" المشهورة لإيجاد حل جاهز للمشاكل في ديناميكية التربة ذو الأبعاد الثنائية . ولقد بسطت معادلة لإيجاد القوة اللازمة باستعمال فرضيات معينة . ثم استخدم مثال لإيجاد القدرة اللازمة في البلدوزر لعمل شغل معين بدفع التربة . ومن المؤمل أن يكون هذا البحث ذو فائدة كبيرة خاصة عند اختيار التصميم الصحيح لسكينة البلدوزر ولهدف محدد .*

## 1. Introduction

A bulldozer is a powerful crawler such as caterpillar tracked tractor equipped with a blade. Tires could replace the track for quick operation. The term bulldozer often used to denote any heavy engineering vehicle although the term officially relates to the dozer blade installed on tractor. The most common usage of the term bulldozer is to denote a tractor (most often tracked) equipped with a blade.

The first bulldozer was adapted from frame tractors that were used to plough fields. In order to dig canals, raise earthen dams, and do other earth moving projects, the tractor was equipped with a large thick metal plate. This thick metal plate, it got its curved shape is called a "blade"<sup>[1, 2]</sup>.

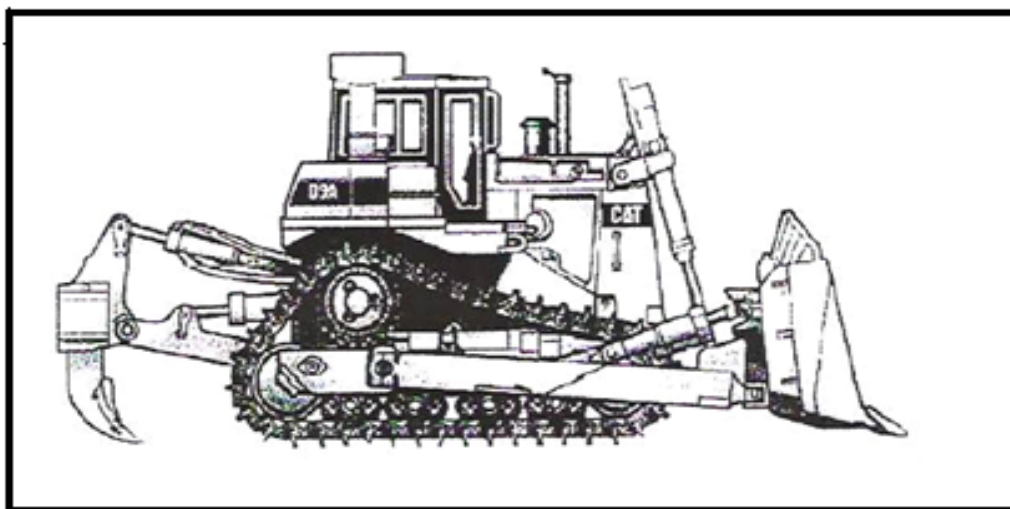


Figure (1): Tracked-type Bulldozer

Through the years, bulldozers got bigger, more powerful, and more sophisticated. The dozer blade is a piece of heavy metal plate, installed on the front of the tractor, with the aim of pushing things, handle rough obstacles and shoving sand, dirt and debris. Bulldozer can be found on large and small scale construction sites, mines, roadsides, military bases, heavy industry factories and large governmental projects<sup>[3, 4, & 5]</sup>.

## 2. Theory

The accurate evaluation of earth pressure on bulldozer blade is of a considerable importance in investigations concerned with soil implemented and soil vehicle mechanics<sup>[6, 7, & 8]</sup>. Reece's has postulated an equation which can be written as follows<sup>[9]</sup>:-

$$P = \gamma z^2 N\gamma + czNc + ca zNa + qzNq \quad \dots(i)$$

Where

- c = apparent cohesion, N/m<sup>2</sup>.
- ca = soil- interface adhesion, N/m<sup>2</sup>.
- N $\gamma$ , Nc, Na, Nq = dimensionless Reece factors .

$P$  = soil reaction per unit width of interface, N/m.

$q$  = surcharge pressure on soil free surface, N/m<sup>2</sup>.

The four terms in this equation represent the gravitational, cohesive, adhesive and surcharge components of the soil reaction per unit width of interface respectively. The N-factors in equation (i) represent pure numbers, which are dimensionless Reece factors. These numbers describe the shape of the soil surface and thus function of angle of shearing resistance  $\phi$ , and soil interface friction angle  $\delta$  and the geometry of the loaded interface.

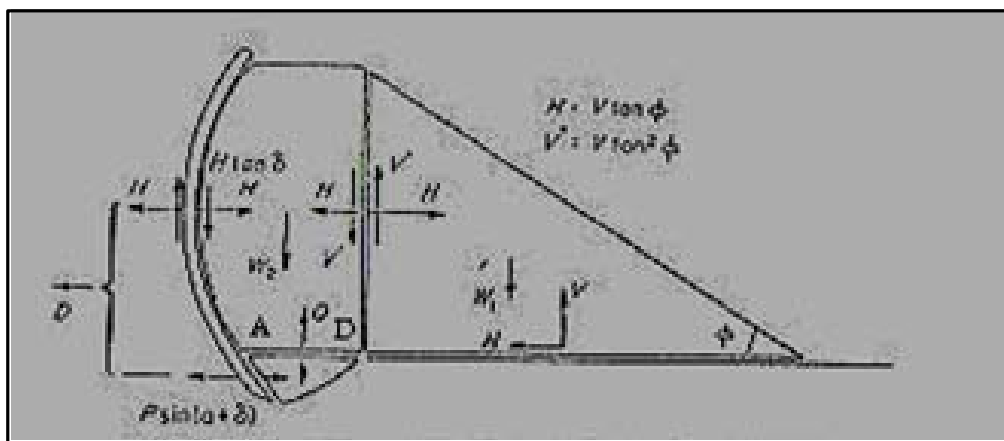
Reece's equation applies to all forms of soil failure where deformation takes place slowly as in bulldozer blades. Thus inertia forces can be neglected. Rearranging equation (i)

$$P = z [\gamma z N_\gamma + c N_c + ca N_a + q N_q] \dots (ii)$$

For simplicity the adhesive components of equation (ii) will be ignored for the time being. This is because it has assumed a very smooth blade as a new design is used. So, as a result, a very simple equation will be obtained as follow:-

$$P = z [z \gamma N_\gamma + c N_c + q N_q] \dots (1)$$

A simplified failure pattern for calculating the draught of a bulldozer is shown in figure (2).



**Figure (2): Simplified Failure Pattern for Calculating the Draught of a Bulldozer**

Frictional force =  $\mu \times$  Normal reaction

Where

$$\mu = \tan \phi = \frac{H}{V} = \frac{V}{H}$$

Where H, V &  $\bar{V}$  are forces shown in figure (2).

If  $W_1$  is the weight of soil triangle per unit width, then

$$W_1 = V + \bar{V} = V + H \tan \phi = V + V \tan \phi \tan \phi$$

$$\therefore W_1 = V [1 + \tan^2 \phi] \quad \dots (2)$$

Also  $W_1 = \text{Area of triangle} \times \gamma \quad \dots (3)$

If  $W_2$  is the soil weight per unit width above rupture distance (AD), then

$$W_2 = \text{Rupture distance (AD)} \times \text{Height} \times \text{density } (\gamma)$$

The values of dimensionless Reece's factors can be calculated as follows:-

$\phi$  is represented by a family of curve increasing in steps of  $5^\circ$  to  $45^\circ$  and  $\delta$  is accounted for only two specific values ( $\delta=0$  and  $\delta = \phi$ ). Two main interpolations are required to cover the N – factors at intermediate values of both  $\phi$  and  $\delta$ .

The following relation ship can be established<sup>[10]</sup> for the required value of appropriate N-factors and using N-factor curves which are shown in figures (3,4,5,6,7,&8).

$$N_\delta = N_{\delta=0} \left[ \frac{N_{\delta=\phi}}{N_{\delta=0}} \right]^{\delta/\phi} \quad \dots (4)$$

Interpolation for  $\delta$  in the range  $0 < \delta < \phi$  can thus be carried out with reasonable accuracy from eqn. (4)

The distance (AD) has been designated the "rupture distance" is often required in the analysis of soil failure problems. The following required rapture distance ratio is calculating from figure (9)

$$m_\delta = m_{\delta=0} \left[ \frac{m_{\delta=\phi}}{m_{\delta=0}} \right]^{\delta/\phi} \quad \dots (5)$$

### 3. Example of application

Since equation (1) can be used to compute the forces involved in the failure of any mass of soil, the values of the N- factors presented in this paper will provide the basis for the solution of number of practical problems.

As a typical example, the following soil & blade values are used

Soil properties:  $\phi = 32^\circ$ ,  $c = 8.63 \text{ kN/m}^2$ ,  $\gamma = 17.95 \text{ kN/m}^3$

Soil – Metal values:  $\delta = 11^\circ$ ,

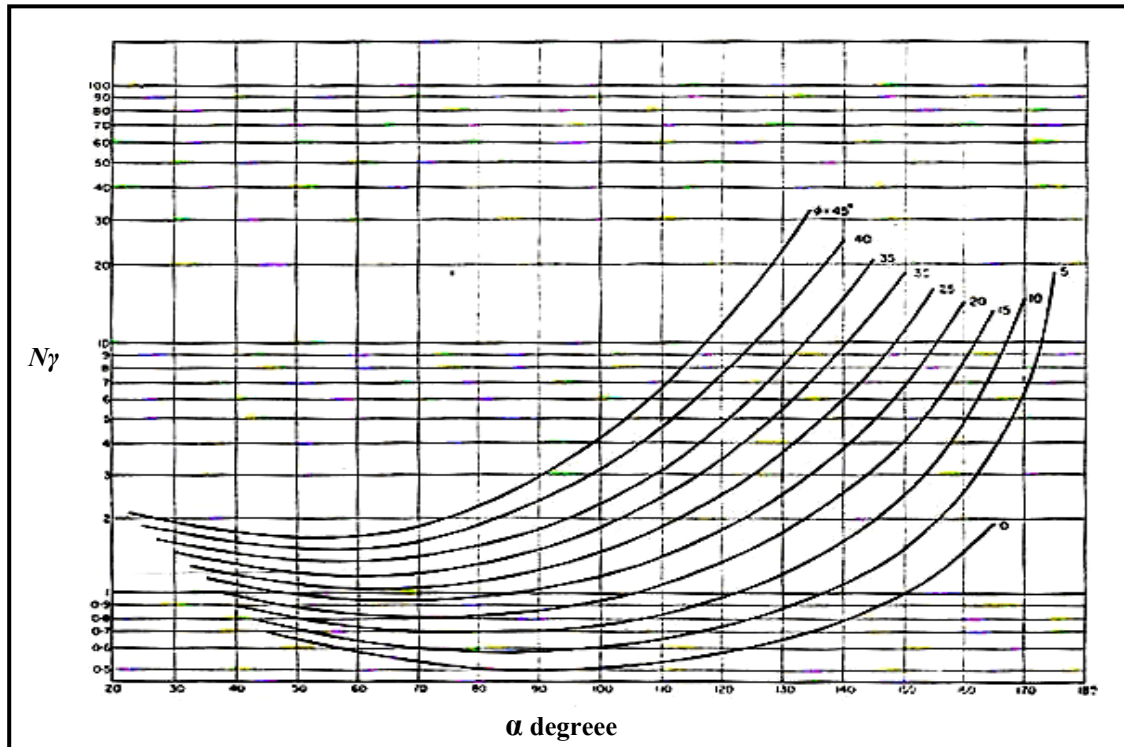
Blade geometry:  $z = 0.15\text{m}$ , total height =  $1.14\text{m}$ , width =  $4.6\text{m}$ ,  $\alpha = 57^\circ$

The value of  $N\gamma$  when  $\delta = 0$  was found equal to 1.25 from figure (3)

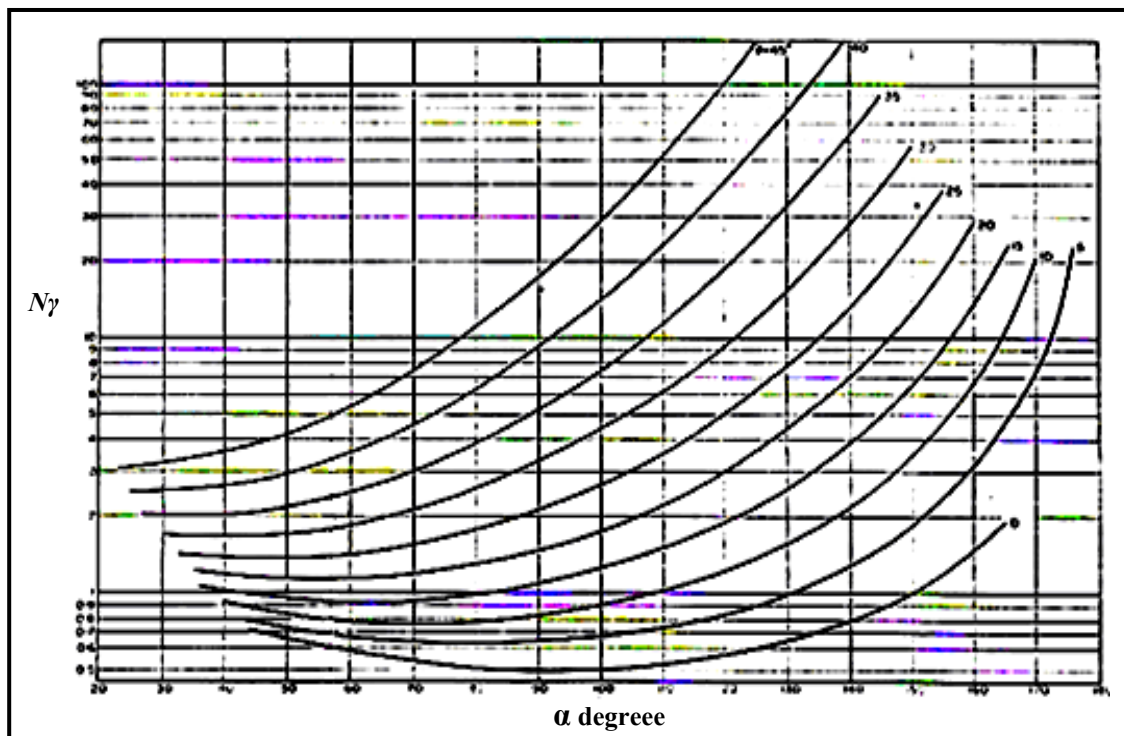
While the values of  $N\gamma$  when  $\delta = \phi$  was found = 2 from figure (4)

And as a result, the actual required value of  $N_\gamma$  when  $\delta=11$  is found using eqn. (4) by method of interpolation therefore

$$N_\gamma = 1.25 \left( \frac{2}{1.25} \right)^{1/32} = 1.47$$



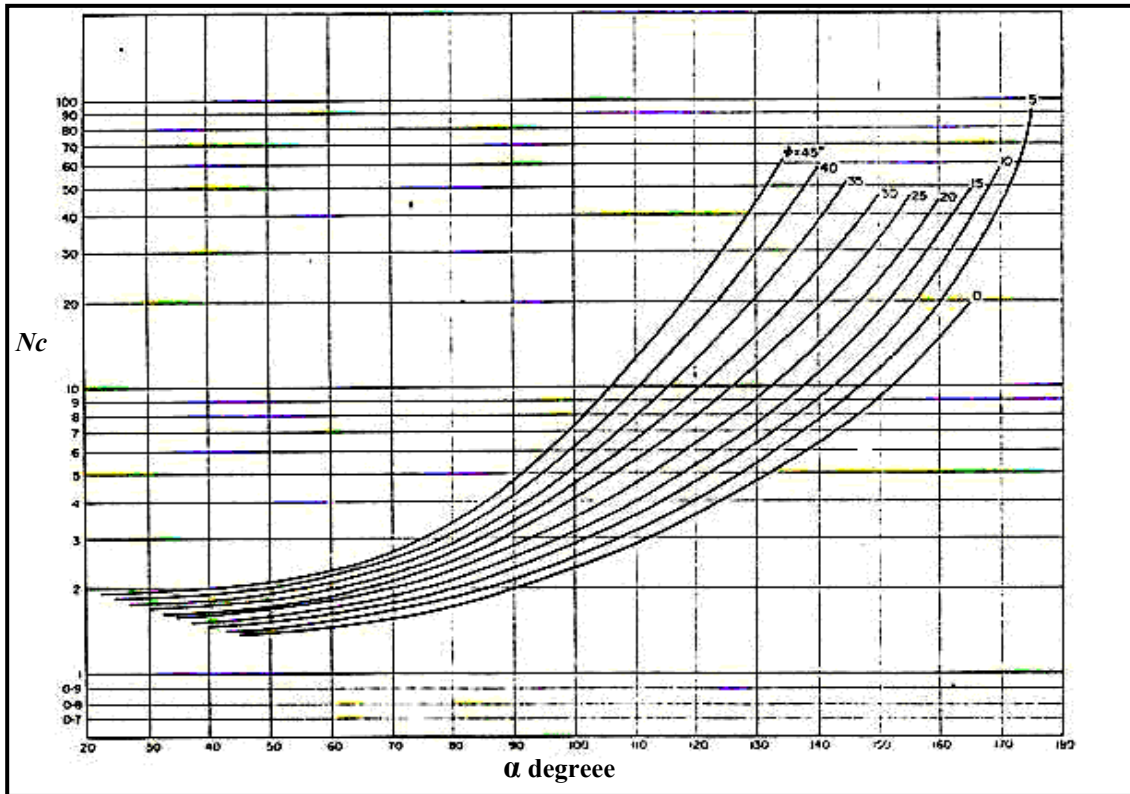
**Figure (3) Relationship between  $N_\gamma$  and  $\alpha$  when  $\delta=0$**



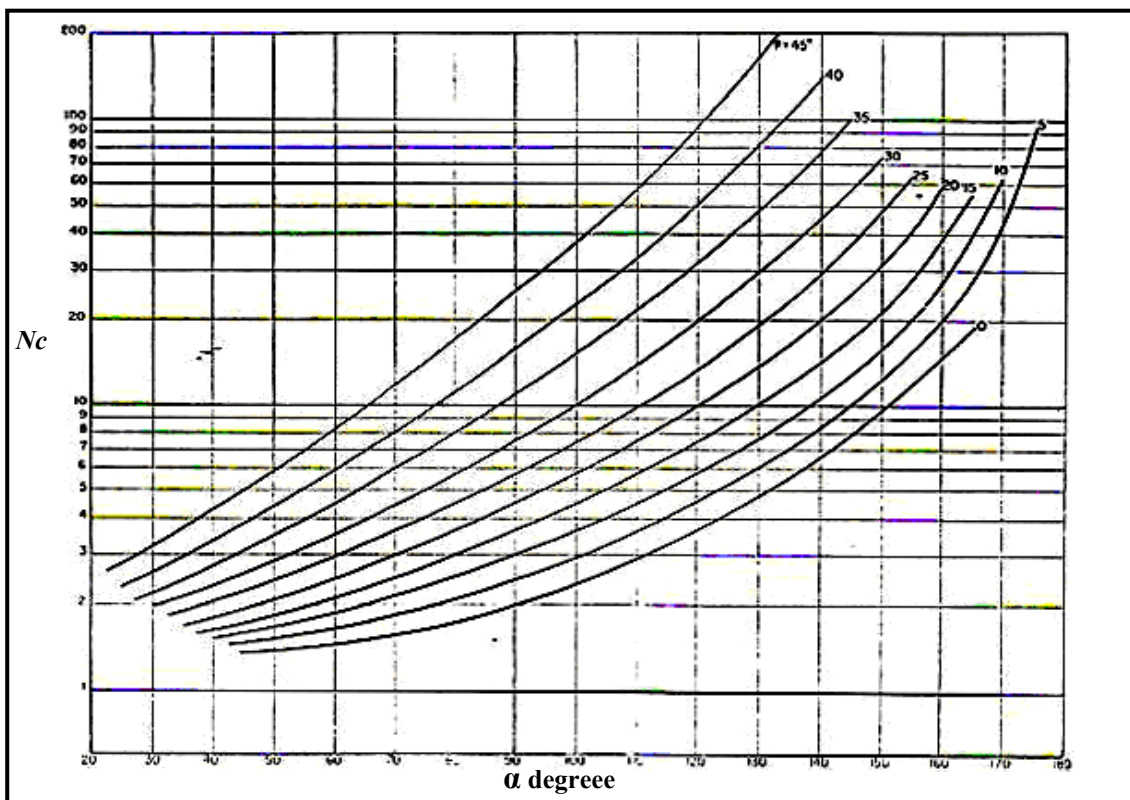
**Figure (4) Relationship between  $N_\gamma$  and  $\alpha$  when  $\delta=\phi$**



Similarly the value of  $N_c$  for  $\delta=0$  was found =1.98 using figure (5) .While the value of  $N_c$  for  $\delta=\phi$  was found =3.6 using figure (6)



**Figure (5) Relationship between  $N_c$  and  $\alpha$  when  $\delta=0$**



**Figure (6) Relationship between  $N_c$  and  $\alpha$  when  $\delta=\phi$**

Hence, the required value for  $N_c$  was calculated as before using eqn (4), and which is  $N_c = 2.43$ . Similarly the value of  $N_q$  when  $\delta = 0$  was found = 2.5 from figure (7) While the value of  $N_q$  for  $\delta = \phi$  was found = 4 using figure (8)

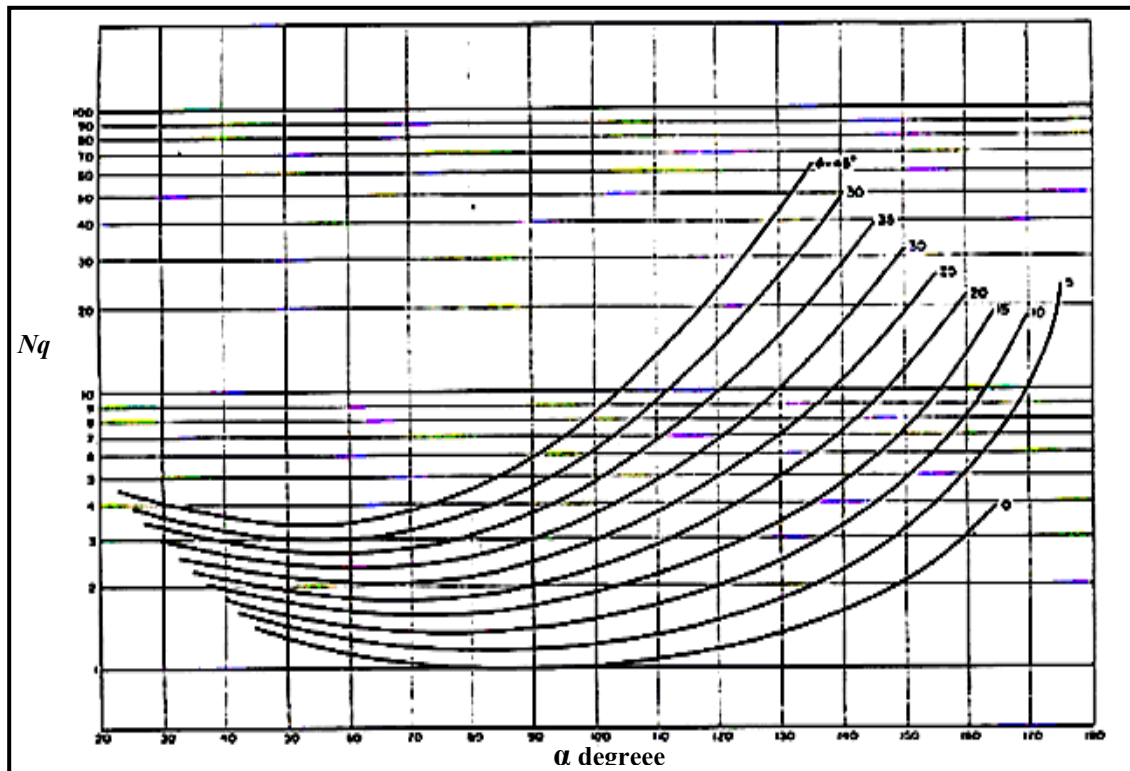


Figure (7) Relationship between  $N_q$  and  $\alpha$  when  $\delta=0$

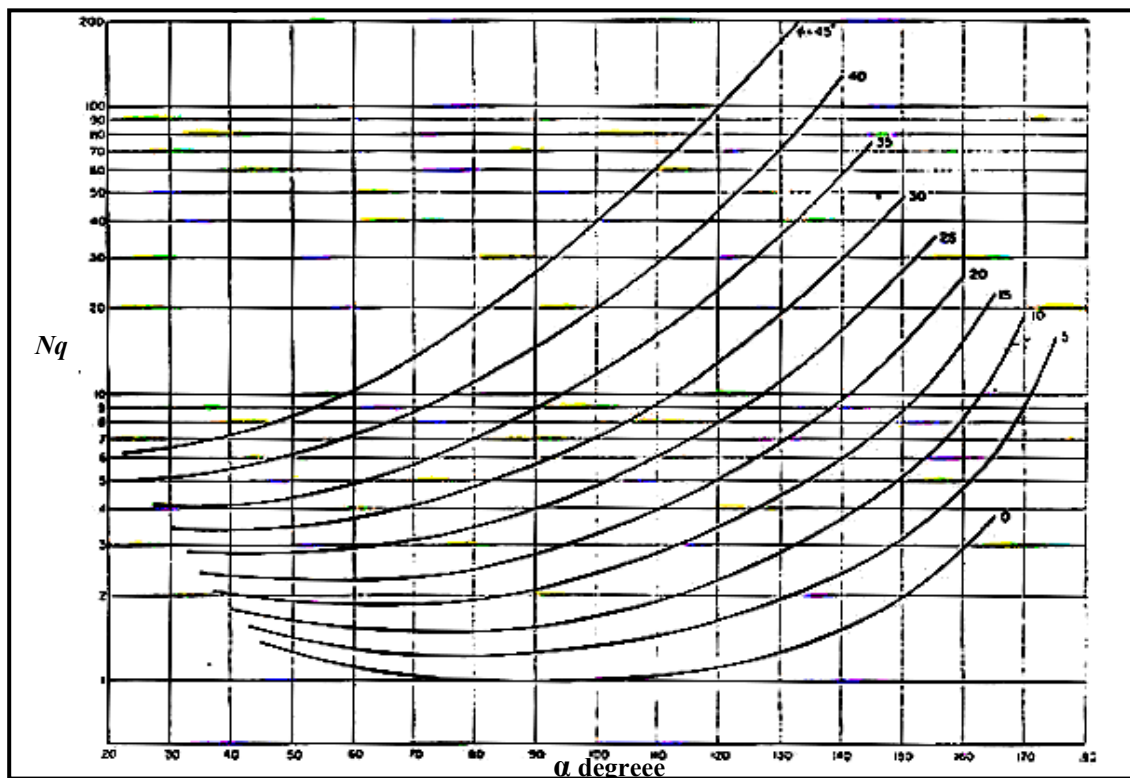


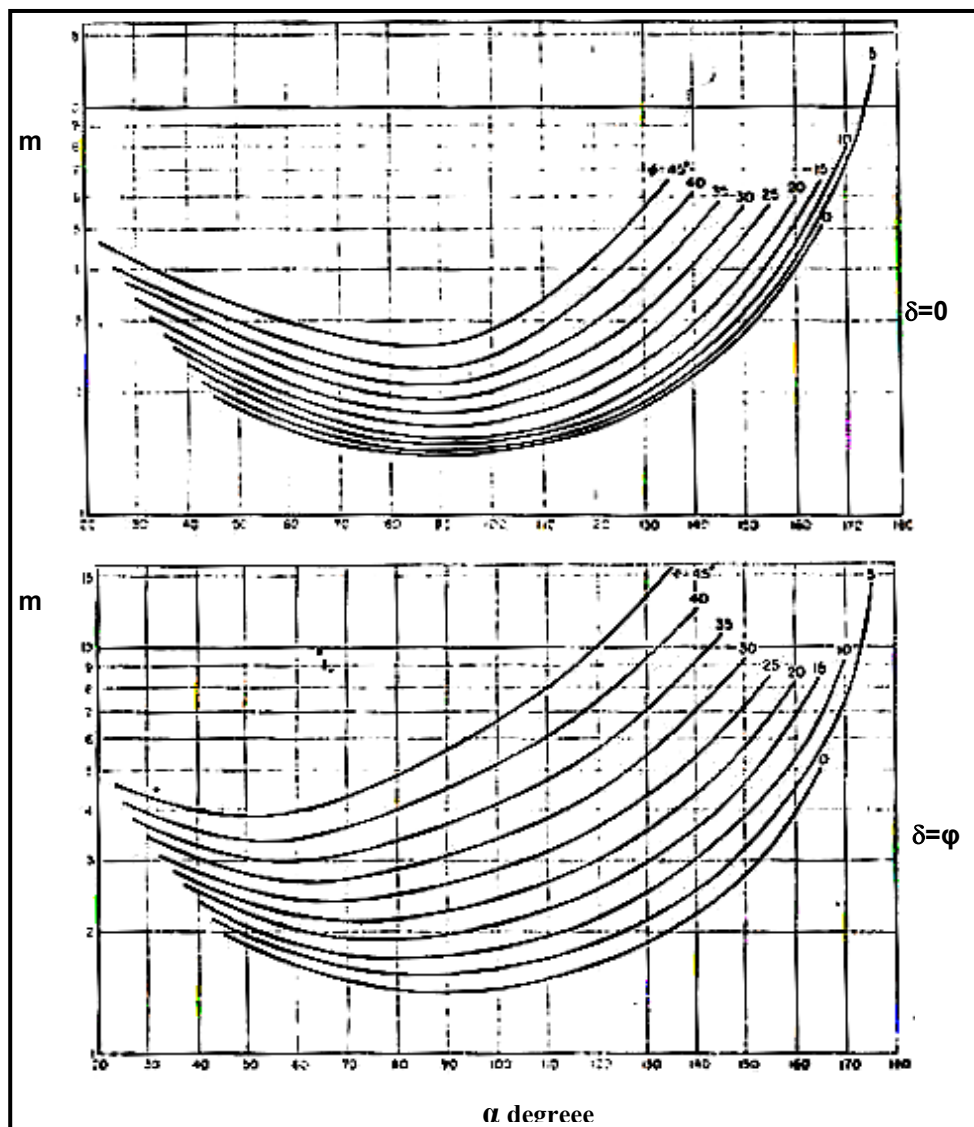
Figure (8) Relationship between  $N_q$  and  $\alpha$  when  $\delta=\phi$

And as before, the required value for  $N_q$  was calculated using eqn (4) which is  $N_q = 2.94$ . To summarize the values of the N- factors obtained by the method of interpolation are given in table (1)

**Table (1) Interpolated N-values**

	Interpolated for $\phi = 32^\circ$		Interpolated for $\delta = 11^\circ$ (eqn.(4))
	$N_{\delta=0}$	$N_{\delta=\phi}$	Calculated N
Gravitational ( $N_\gamma$ )	1.25	2.00	$N_\gamma = 1.47$
Cohesive ( $N_c$ )	1.98	3.60	$N_c = 2.43$
Surcharge ( $N_q$ )	2.50	4.00	$N_q = 2.94$

Finally the rupture distance ratio was found using figure (9)



**Figure (9) Mean Ratio of Rupture Distance to Depth when  $\delta=0$  (top) and  $\delta= \phi$  (bottom)**



The rupture distance ratio ( $m$ ) has been interpolated from Eqn. (5)

$$m = 2.45 \left( \frac{2.70}{2.45} \right)^{11/32} = 2.54$$

The rupture distance ( $AD$ ) =  $m \times z = 2.54 \times 0.15 = 0.381$  m

From dimensions given in fig (2) the following value can be computed for unit width of blade

$$W_1 = \text{Area of triangle} \times \gamma$$

Where the height of triangle = height of blade – depth of blade  
 =  $1.14 - 0.15 = 0.99$  m

$$\text{The base of triangle} = \frac{0.99}{\tan \varphi} = 1.58 \text{ m}$$

$$\therefore W_1 = \frac{1.58 \times 0.99}{2} \times 17.95 = 14 \text{ kN/m}$$

From eqn. (2)

$$V = \frac{W_1}{1 + \tan^2 \varphi}$$

$$= \frac{14}{1 + \tan^2 32} = 10 \text{ kN/m}$$

$$W_2 = (AD) \times \text{height} \times \gamma = 0.381 \times 0.99 \times 17.95 = 6.75 \text{ kN/m}$$

$$q = [W_2 + V \tan \varphi (\tan \varphi + \tan \delta)] / (AD) = 31.15 \text{ kN/m}^2$$

Substituting these values in eqn (1)

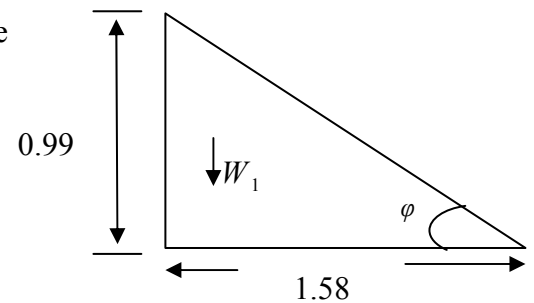
The total draught per unit width is equal to:-

$$P \sin (\alpha + \delta) + V \tan \varphi$$

$$\therefore \text{Total draught force } D = [(z^2 N\gamma + czNc + qzNq) \times \sin (\alpha + \delta) + V \tan \varphi] \times \text{width} = 103.28 \text{ kN}$$

If an assumed average speed of bulldozer is 5 km/h, then the required horsepower to do this job is =  $103.28 \times 10^3 \times (5 / 3.6)$  Nm/s

$$= 143.4 \text{ kW (188 Hp)}$$



#### 4. Conclusion

It has been shown with given data of soil and Bulldozer blade shape, the total required draught force can be calculated theoretically. This was accomplished using valuable Reece's family of curves which have been already well established. Thus the required horse power for bulldozer to push soil in front of the blade can be estimated given the speed of the bulldozer. Regarding this work there are almost no published papers or research activities have been done in Iraq. Therefore and as a result, it is hoped that this paper with the given example will be useful in selecting the optimum design for a required job.

## Notations

- $c$  = apparent cohesion, N/m<sup>2</sup>.  
 $c_a$  = soil- interface adhesion, N/m<sup>2</sup>.  
 $(AD)$  = rupture distance, m.  
 $m$  = ratio of rupture distance to depth of cut.  
 $N_\gamma, N_c, N_a, N_q$  = dimensionless Reece factors.  
 $P$  = soil reaction per unit width of interface, N/m.  
 $q$  = surcharge pressure on soil free surface, N/m<sup>2</sup>.  
 $W_1$  = weight of soil triangle per unit width in front of Bulldozer, N/m.  
 $W_2$  = weight of soil above rupture distance (AD) per unit width, N/m.  
 $W$  =  $W_1 + W_2$  , N/m.  
 $z$  = depth of cut, m.  
 $\alpha$  = rake angle of interface, deg.  
 $\gamma$  = bulk density of soil, N/m<sup>3</sup>.  
 $\delta$  = angle of soil – interface friction, deg.  
 $\phi$  = angle of shearing resistance, deg.  
 $\mu$  = coeff .of friction between soil layers.  
 $H$  = horizontal reaction per unit width between blade & soil, N/m.  
 $V$  = vertical reaction of soil triangle per unit width, N/m.  
 $\bar{V}$  = frictional force between soil triangle & soil prism per unit width, N/m.  
 $D$  = total required draught force, N.

## **5. References**

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